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Effects of an Inclined Cente red Conductor on MHD Natural and Forced Convection Within a Heated Wavy Chamber

S. O. Juma a* , J. K. Sigey a* , J. O. Abonyo ^a and S. K. Maritim ^b

^a Department of Pure and Applied Mathematics, Jomo Kenyatta University of Agriculture and Technology, Nairobi, Kenya. ^b Department of Mathematics and Computer Science, Bomet University College, Bomet, Kenya.

Authors' contributions

This work was carried out in collaboration among all authors. All authors read and approved the final manuscript.

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Abstract

The study of the effect of hall and ion slip on an inclined conductor on MHD natural and forced convection in a heated wavy chamber with a constant transversal magnetic field applied. The governing momentum and energy equation were solved by applying finite central scheme approximation and the resulting partial difference equations were solved by MATLAB software. The study showed that an increase heat absorption coefficient lowers the surface heat transfer thus lowering flow rate. An increase in Rayleigh number increases the flow rate while an increase in the angle of inclination of the conductor increases the buoyancy force component thereby increasing the flow rate. The results further showed that flow rate became higher at an inclination angle of 90º. In addition, the results also showed that an increase in Hartmann increases the flow rate. The Hartmann number, Rayleigh number and Absorption coefficient are analytically discussed and represented in tables and graphical profiles with respect to flow velocity and temperature profile due to engineering demand. This current study a direct application in the development of MHD propelled vessels in the marine and space-craft department.

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^{}Corresponding author: Email: 1samson.juma@students.jkuat.ac.ke, jksigey@jkuat.ac.ke;*

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Nomenclature

- *ɷ : Angle of inclination.*
- *B⁰ : Magnetic field strength*
- *g : Gravitational field strength.*
- *u, v : Velocity components in x and y direction respectively (m/s).*
U, V : Dimensionless velocity components along x and y axis.
- *U, V : Dimensionless velocity components along x and y axis.*
- *T : Thermodynamic temperature (Kelvin)*
- *x, y : Cartesian coordinates.*
- *Pr : Prandtl number*
- *Ra^T : Thermal Rayleigh number*
- *Gr : Grash of number*
- f : Density (kg/m³)
- *Re : Reynolds number*
- *P : Static pressure (N/m²)*
- *Nu : Nusselt number*
- *T : Thermodynamic temperature.*
- *Ha : Hartmann Number*
- *N^c : Buoyancy ratio*

Abbreviations

- *MHD : Magneto-Hydrodynamic*
- *CDS : Central Difference Scheme*
- *PDE : Partial Differential Equation*

Greek Symbols

- *α : Thermal diffusivity (m² /s)*
- *σ : Electrical conductivity (Ohm-metre)*
- *k : Thermal conductivity (W/M/K)*
- *ϕ : Absorption coefficient (1/cm)*
- *β : Fluid thermal expansion coefficient (1/K)*

1 Introduction

Magneto hydrodynamic flow, which is the mass transfer of electrically conductive fluids within a magnetic field, is of vital importance both internationally and locally in the marine and aircraft depart among other sectors of engineering where it's gained massive application. In the department of Marine and Aircraft, many researchers have tried to solve the problem. As charges flow through a magnetic field, they give rise to some thrust force whose magnitude depends on the angle of inclination between the two fields from (Flemings' $19thC$). The force experienced between a conductive fluid and a magnetic field during a MHD convective flow can be used to develop vessels which are non-mechanical and easier to operate, non – pollutant since they don't use combustible fuel as their propelling mechanism. This force that depends on many factors which this study has looked at is found to be acting perpendicularly in direction to the two fields. It is because of this reason that the MHD convective flow knowledge becomes relevant to the marine and space craft department since the vessels developed are very fast, easy to manoeuvre, economical, and environmentally friendly to operate unlike the mechanical vessels. Therefore, how to increase the induced force during MHD flow has been the basis of most of studies.

Nasrin [1] studied the effects of a conducting obstacle centred on MHD combined convection in a wavy chamber. The result showed that Richardson number (Ri) and the diameter (D) of the conducting obstacle strongly affect the flow phenomenon.

Khantun *et al.* (2018), numerically investigated the magneto hydrodynamic free convection fluid flow over an upright permeable plate with induced magnetic field. The results obtained showed that the velocity profile decreases with an increase in Prandtl number, magnetic parameter (m) and Schmidt number (S_c). Roizaini *et al.* (2020), investigated magnetic field effects on mixed convection heat transfer in a lid – driven rectangular cavity. The result of the study showed that Hartmann number has a significant effect on the convective current. Arash Karimipour *et al.* [2], investigated the magnetic field influence on combined convection heat transfer in a liddriven rectangular enclosure. The results of the study showed that Hartmann number significantly affects the fluid flow structure and temperature field. Absana *et al.* (2021) investigated a two-dimensional unsteady MHD free convection flow over a vertical plate in the presence of radiation. The results of their study showed that the velocity profile of the flow decreases with an increase in radiative parameter while the velocity profiles reduced with an increase in Prandtl number. Smith *et al* [3], investigated the influence of centred conducting body on natural convection heat transfer in an enclosure. The results of their findings showed that fluid flow and heat transfer processes are governed by Rayleigh and Prandtl numbers, the dimensionless body size and the ratio of the thermal conductivity of the body. Singh A. K. [4], studied the numerical solution of hydro-magnetic non-steady free convection flow past an infinite permeable plate. The results showed that Prandtl number or magnetic parameter strongly affects the skin friction while the reverse effect was noted for an increase in suction parameter. Sigey *et al.* [5], investigated MHD free convective flow past an infinite vertical porous plate with joule heating effect. The result showed that an increase in joule heating parameter causes an increase in temperature and velocity profile. Sarris *et al.* [6], investigated MHD free convection in sideways and volumetrically heated square cavity. The results indicated that the flow profile is influenced by Rayleigh and Hartmann number. Sagheer *et al*. [7], numerically investigated MHD mixed convection and entropy generation of water alumina nano-fluid flow in a double lid driven enclosure with discrete heating. It was found that Reynolds and Hartmann numbers, volume fraction and angle of magnetic inclination strongly affects the flow. Basak and Roy [8], investigated finite element analysis of free convection flow in a square enclosure with differently heated walls. The results showed that Prandtl and Rayleigh numbers greatly affect the velocity and temperature profile. Mahdy *et al*. [9], studied MHD mixed convection in a tilted lid – driven enclosure with opposing thermal buoyancy force. It was found that the flow is reduced by the presence of magnetic field and the average Nusselt number is an increasing function of the magnetic field angle. Oztop *et al*. [10] investigated mixed convection of nano – fluid filled cavity with oscillating lid under the influence of an inclined magnetic field. The results showed that Strouhal, Richardson and Hartmann numbers greatly affect the heat transfer process. Moreau *et al*. [11], studied free convection in a rectangular cavity with a horizontal magnetic field. The results showed that the velocity profile varies with the Hartmann number [12,13]. From the above literatures, it can be seen that there is no significant information on the effect of the angle of inclination of a centred conductor on MHD free and forced convection. The current study addresses this problem. The specific objectives of the study are:

- i. To formulate a mathematical model for the effects of an inclined conductor on MHD natural and forced convection in a heated wavy chamber.
- ii. To determine the effect of the angle of inclination on temperature distribution.
- iii. To determine the influence of magnetic field on temperature distribution profile.
- iv. To determine the effects of flow parameter on temperature and velocity profile distribution.

2 Model Specification

The set-up below consists of a two-dimensional lid-driven rectangular chamber of length P. The upper and lower parts of the cavity are insulated, the left lid is at a uniform velocity and the temperature $T_i (20^{\circ}C)$, while the right wall with a temperature T_h (100°C). The conductor is tilted through an angle (ω) for (30° $\leq \omega \leq 90^{\circ}$) along the horizontal axis within a conductive fluid taken as air of $(Pr = 0.71)$. A constant magnetic field of strength B_0 is applied in the horizontal direction to the sidewalls of the chamber

Fig. 1. The schematic diagram

T is the temperature, and B_0 is the external magnetic field strength.

2.1 Assumptions

In order to solve and analyse this occurrence, the following assumptions are made:

- i. The flow is steady, laminar, 2-D and incompressible.
- ii. The earth's magnetic effects are negligible
- iii. There is no radiation effect.
- iv. Magnetic effect is only experienced in the horizontal direction.
- v. The magnetic field meets the centred conductor perpendicularly.
- vi. There is no magnetic dissipation since the external magnetic field is a mono- pole with no other magnetic field interaction.

3 Mathematical Formulation

The flow is assumed to be laminar, steady and incompressible and that magnetic effect only acts horizontally.

3.1 Natural convection

The specific momentum equation for this case will be obtained by considering Newton's second law. The external forces acting on the fluid under this case are the buoyancy and magnetic force.

Equation along x – axis

along x-axis
\n
$$
u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho} \frac{\partial p}{\partial x} + v \left[\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right] + \sin \omega g \beta \tau [T - T_c]
$$
\n(1)

Equation along y-axis

along y-axis
\n
$$
u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho} \frac{\partial p}{\partial y} + v \left[\frac{\partial^2 v}{\partial x^2} + v \frac{\partial^2 v}{\partial y^2} \right] + \cos \omega g \beta_T \left[T - T_c \right] - \frac{k \sigma \beta_0^2 v}{\rho}
$$
\n(2)

12

Enegy equation

$$
u\frac{\partial T}{\partial x} + v\frac{\partial T}{\partial y} = \alpha \left[\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right] + \frac{Q_0}{\rho C_p} (T - T_c)
$$
\n(3)

3.2 Forced convection

In this type of convection, there is a mass movement or fluid movement due to an external forcing condition.

Momentum along x-axis

$$
u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = v\frac{\partial^2 u}{\partial x^2} + \sin \omega \tag{4}
$$

Momentum along y-axis.

$$
u\frac{\partial v}{\partial x} + v\frac{\partial v}{\partial y} = v\frac{\partial^2 v}{\partial y^2} + \cos\omega - \frac{k\sigma\beta_0^2 v}{\rho}
$$
\n(5)

Energy equation.

$$
u\frac{\partial T}{\partial x} + v\frac{\partial T}{\partial y} = \alpha \left[\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right] + \frac{Q_0}{\rho C_P} (T - T_c)
$$
\n(6)

Introducing initial boundary conditions.

With initial boundary conditions:

 $u = 0, v = v_o, T = T_i$ vertical walls

At horizontal wall: $u = 0$, $v = 0$, $\frac{\partial T}{\partial n} = 0$

At the wavy surface: $u = 0$, $v = 0$, $T = T_n$

At the solid-fluid interface
$$
\left(\frac{\delta T}{\delta n}\right)_{fluid} = \frac{\kappa_s}{\kappa} \left(\frac{\delta T}{\delta n}\right)_{solid}
$$

The rate of heat transfer on the wavy wall is expressed in terms of Nusselt number

 $\ddot{}$

$$
\overline{Nu} = \frac{\text{Convective heat transfer}}{\text{conductive heat transfer}} = \frac{h}{K/L} = \frac{hl}{K} = \frac{\partial T}{\partial n}L
$$

Introducing non-dimensional numbers:

$$
X = \frac{x}{L}, Y = \frac{y}{L}, U = \frac{UL}{\alpha}, V = \frac{vL}{\alpha}, Pr = \frac{pL^2}{\rho \alpha^2}
$$

\n
$$
\theta = \frac{T - T_c}{T_h - T_c}, Pr = \frac{v}{\alpha}, \alpha = \frac{K}{\rho c_p}, \sigma = \frac{\rho L^2}{L^2}
$$

\n
$$
Ha^2 = \frac{\sigma B_o^2 L^2}{\mu}. \quad Ra = \frac{g \beta L^3 (T_n - T_c) Pr}{V^2}, \sigma = \frac{\rho^2 \alpha}{L^2}, \alpha = \frac{K}{\rho c_p}
$$

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Momentum along x-axis

nentum along x-axis
\n
$$
U\frac{\partial U}{\partial X} + V\frac{\partial U}{\partial Y} = -\frac{\partial P}{\partial X} + \text{Pr}\left[\frac{\partial^2 U}{\partial X^2} + \frac{\partial^2 U}{\partial Y^2}\right] + \sin \omega \left(Rar \text{Pr}\left[\theta - N_c\right]\right)
$$
\n(7)

Equation along y – axis

$$
\begin{aligned}\n\text{ation along } \mathbf{y} - \mathbf{axis} \\
U \frac{\partial V}{\partial X} + V \frac{\partial V}{\partial Y} &= -\frac{\partial P}{\partial Y} + \Pr\left[\frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2}\right] + \cos \omega \left[R_{\alpha T} \Pr\left(\theta - \mathbf{N}_c\right) - Ha^2 \Pr V\right] \\
&\tag{8}\n\end{aligned}
$$

Energy Equation.

The specific energy equation is obtained from the first law of Thermodynamics where Φ is the heat absorption coefficient.

$$
U\frac{\partial \theta}{\partial X} + V\frac{\partial \theta}{\partial Y} = \left[\frac{\partial^2 \theta}{\partial X^2} + \frac{\partial^2 \theta}{\partial Y^2}\right] + \Phi \theta
$$
\n(9)

3.3 Forced convection

The dimensionless equation for this case becomes:

Equation along x -axis

$$
U\frac{\partial U}{\partial X} + V\frac{\partial U}{\partial Y} = \Pr\left[\frac{\partial^2 U}{\partial X^2}\right] + \sin \omega \tag{10}
$$

Equation along y -axis

$$
U\frac{\partial V}{\partial X} + V\frac{\partial V}{\partial Y} = \Pr\left[\frac{\partial^2 V}{\partial Y^2}\right] + \cos\omega - Ha^2 \Pr V
$$
\n(11)

4 Method of Solution

The problem under investigation generates partial differential equations whose solutions are to be determined using the finite difference approach. The momentum and energy equations are solved using the Finite central scheme technique. All the four nodes (which are obtained from a uniform mesh of square with reference to the central node) of velocity components U and V and temperature θ are the basic unknowns. The resulting pairs of linear simultaneous equations are then solved by MATLAB simulation software under a set of boundary conditions.

Discretization of momentum equation a long x axis

We consider Momentum Equation a long x axis (7) and use it to investigate the fluid velocity profiles. For the central scheme (CDS), the values, U_x , U_y , U_{xx} and U_{yy} are replaced by the central difference approximation.

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$$
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$$

$$
u\left(\frac{U_{i+1,j} - U_{i-1,j}}{2\Delta x}\right) + v\left(\frac{U_{i,j+1} - U_{i,j-1}}{2\Delta y}\right) = \left(\frac{U_{i+1,j} - 2U_{i,j} + U_{i-1,j}}{(\Delta x)^2} + \frac{U_{i+1,j+1} - 2U_{i,j+1}}{(\Delta y)^2}\right) + \sin \omega \left(Ra_r \Pr(\theta - N_c)\right)
$$
(12)

Take $U = V = N_c = \theta = 1$, multiply both sides by $2(\Delta x)$ and let Pr = 0.71 and take $\Delta x = \Delta y = 0.1$ on a square mesh into equation (12) we get the scheme; The U = V = N_C = θ = 1_{, multiply both sides by 2^(Δx) and let Pr = 0.71 and take $\Delta x = \Delta y = 0.1$ on a square nesh into equation (12) we get the scheme;
0.86U_{_{i+1,j} + 8U_{i,j} - 1.14U_{i+1,j} = -0.86U_{i,j+1} + 1.1}}

$$
0.86U_{i+1,j} + 8U_{i,j} - 1.14U_{i-1,j} = -0.86U_{i,j+1} + 1.14U_{i,j-1} + \sin\omega\left(Ra_T\Pr\left(\theta - N_c\right)\right)
$$
(13)

Taking $i = 1,2,3, \ldots, 5$ and $j = 1$ we form the following systems of linear algebraic equation,

And with initial and boundary conditions $U_{i,0} = U_{0,j} = 1$ and $U_{i,2} = 0$ respectively, the above algebraic equations (13) can be written in matrix form as;
 $\begin{bmatrix} 8 & 0.86 & 0 & 0 & 0 \ 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} U_{1,1} \ U_1 \end{b$ equations (13) can be written in matrix form as;

ations (13) can be written in matrix form as;
\n
$$
\begin{bmatrix}\n8 & 0.86 & 0 & 0 & 0 \\
-1.4 & 8 & 0.86 & 0 & 0 \\
0 & -1.4 & 8 & 0.86 & 0 \\
0 & 0 & -1.4 & 8 & 0.86 \\
0 & 0 & 0 & -1.4 & 8\n\end{bmatrix}\n\begin{bmatrix}\nU_{1,1} \\
U_{2,1} \\
U_{3,1} \\
U_{4,1} \\
U_{5,1}\n\end{bmatrix} =\n\begin{bmatrix}\n0.14 + 0.7 \sin \omega R a_r \\
0.07 + 0.7 \sin \omega R a_r\n\end{bmatrix}
$$
\n(14)

We use equation (14) to investigate the effects of ω and Ra_T on the horizontal fluid velocity profile.

Discretization of momentum equation a long y axis

We consider Momentum Equation a long y axis (8) and use it to investigate the fluid velocity profiles. For the central scheme (CDS), the values, V_x , V_y , V_{xx} and V_{yy} are replaced by the central difference approximation. On substituting these values into Equation (8), it gives;
 $u\left(\frac{V_{i+1,j} - V_{i-1,j}}{V_{i+1,j} - V_{i-1,j}}\right) + v\left$

Central scheme (CDS), the values,
$$
\lambda
$$
, λ , and λ are replaced by the central difference approximation. On substituting these values into Equation (8), it gives:

\n
$$
u\left(\frac{V_{i+1,j} - V_{i-1,j}}{2\Delta x}\right) + v\left(\frac{V_{i,j+1} - V_{i,j-1}}{2\Delta y}\right) = \left(\frac{V_{i+1,j} - 2V_{i,j} + V_{i-1,j}}{(\Delta x)^2} + \frac{V_{i+1,j+1} - 2V_{i,j+1}}{(\Delta y)^2}\right) + \cos\omega\left(Ra_T \Pr(\theta - N_c)\right) - 0.7Ha^2 V_{i,j}
$$
\n(15)

Take $U = V = N_c = \theta = 1$, multiply both sides by $2(\Delta x)$ and let Pr = 0.71 and take $\Delta x = \Delta y = 0.1$ on a square mesh into equation (15) we get the scheme; Take $U = V = N_C = \theta = 1$, multiply both sides by $2(\Delta x)$ and let $Pr = 0.71$ and take $\Delta x = \Delta y = 0.1$ on a square mesh into equation (15) we get the scheme;
0.86 $V_{i+1,j} + (8 + Ha^2)V_{i,j} - 1.14V_{i-1,j} = -0.86V_{i,j+1} + 1.14V_{i,j-1} + \cos \omega (Ra_T \$

$$
0.86V_{i+1,j} + (8 + Ha^2)V_{i,j} - 1.14V_{i+1,j} = -0.86V_{i,j+1} + 1.14V_{i,j-1} + \cos\omega\left(Ra_T \Pr(\theta - N_c)\right)_{\text{(16)}}
$$

Taking and $i = 1,2,3,......$ and $j = 1$ we form the following systems of linear algebraic equations and with initial and boundary conditions $V_{i,0} = V_{0,j} = 1$ and $V_{i,2} = 0$ respectively, the above equation in its matrix form comes to:

16 () () () () () 2 1,1 2 2,1 2 3,1 2 4,1 2 5,1 8 0.86 0 0 0 0.14 0.7cos 1.4 8 0.86 0 0 0.07 0.7cos 0 1.4 8 0.86 0 0.07 0.7cos 0 0 1.4 8 0.86 0.07 0.7cos 0.07 0.7cos 0 0 0 1.4 8 *T T T T T Ha V Ra Ha V Ra Ha V Ra Ha V Ra Ha V Ra* ⁺ ⁺ − + ⁺ − + = ⁺ − + ⁺ ⁺ − + (17)

We use equation (17) to investigate the effects of $H\alpha^2$, ω and Ra_T on the vertical fluid velocity profile.

Discretization of Energy Equation

We consider Energy Equation (9) and use it to investigate the fluid temperature distribution. For the central scheme (CDS), the values, θ_x , θ_x , θ_x and θ_{yy} are replaced by central difference approximation. When these values are substituted into Equation (9), we get;
 $u\left(\frac{\theta_{i+1,j} - \theta_{i-1,j}}{\theta_{i+1,j}}\right) + v\left(\frac{\theta_{i,j+1} - \theta$ values are substituted into Equation (9), we get;

substituted into Equation (9), we get:
\n
$$
u\left(\frac{\theta_{i+1,j} - \theta_{i-1,j}}{2\Delta x}\right) + v\left(\frac{\theta_{i,j+1} - \theta_{i,j-1}}{2\Delta y}\right) = \left(\frac{\theta_{i+1,j} - 2\theta_{i,j} + \theta_{i-1,j}}{(\Delta x)^2} + \frac{\theta_{i+1,j+1} - 2\theta_{i,j+1}}{(\Delta y)^2}\right) + \Phi \theta_{i,j}
$$
\n(18)

Take, multiply both sides by 2^(Δx) and let Pr = 0.71 and take $\Delta x = \Delta y = 0.1$ on a square mesh into equation (18) we get the scheme;
-19 θ _{i+1,j} + (80 - 0.2 ϕ) θ _{i,j} - 21 θ _{i-1,j} = 19 θ _{i,j+1} + 21 θ _i (18) we get the scheme;

$$
-19\theta_{i,j} + (80-0.2\phi)\theta_{i,j} - 21\theta_{i,j+1} = 19\theta_{i,j+1}
$$
 (19)

Taking and $i = 1,2,3,......$ 5 and $j = 1$ we form the following systems of linear algebraic equations and with initial boundary conditions and with initial and boundary conditions $\Theta_{i,0} = \Theta_{0,j} = 1$ and $\Theta_{i,2} = 0$ respectively, the above algebraic equation in its matrix form becomes: mg and $i = 1,2,3,......5$ and $j = 1$ we form the following systems of linear algebraic equations and with
dary conditions and with initial and boundary conditions $\theta_{i,0} = \theta_{0,j} = 1$ and $\theta_{i,2} = 0$ respectively , the
praic e

\n taking and
$$
i = 1, 2, 3, \ldots, 5
$$
 and $j = 1$ we form the following systems of linear algebraic equations and with initial boundary conditions and with initial and boundary conditions $\Theta_{i,0} = \Theta_{0,j} = 1$ and $\Theta_{i,2} = 0$ respectively, the above gebraic equation in its matrix form becomes:\n

\n\n $\begin{bmatrix}\n (8-0.2\Phi) & 0.86 & 0 & 0 \\
 -1.4 & (8-0.2\Phi) & 0.86 & 0 & 0 \\
 0 & -1.4 & (8-0.2\Phi) & 0.86 & 0 \\
 0 & 0 & -1.4 & (8-0.2\Phi) & 0.86 \\
 0 & 0 & -1.4 & (8-0.2\Phi) & 0.86 \\
 0 & 0 & -1.4 & (8-0.2\Phi) & 0.86\n \end{bmatrix}\n \begin{bmatrix}\n \theta_{1,1} \\
 \theta_{2,1} \\
 \theta_{3,1} \\
 \theta_{4,1} \\
 \theta_{5,1}\n \end{bmatrix}\n =\n \begin{bmatrix}\n 420 \\
 210 \\
 210 \\
 210 \\
 210 \\
 210 \\
 210 \\
 200\n \end{bmatrix}$ \n

We use equation (20) to investigate the effects of Φ , on the temperature distribution.

The next chapter details the results obtained for the effects of ω , Φ and Ra_T on the horizontal, vertical fluid velocity profiles and temperature distribution. The results are presented in tables and discussed graphically.

Code validation

The outcome of the present numerical code is pegged against the numerical result of B.A Odongo *et.al* (2021) which was reported for MHD mixed convection flow of a centered conducting obstacle. The comparison is conducted while considering the dimensionless parameters Ha = 10, 11 and 12 and Gr = 0.5, 0.8 and 1.0 Present result for angle of inclination on flow velocity is shown in Fig. 2, which is in agreement with that of B.A Odongo *et.al* (2021). This justifiation gives the assurance in this numerical code under the stated objective.

5 Results and Discussion

In the current study, the Rayleigh number, Hartmann number, angle of inclination and the Absorption coefficient are varied within a constant Prandtl number $Pr = 0.71$. In this section, we consider the effect of Rayleigh and Hartmann number, angle of inclination on velocity profile components as well as the impact of Absorption coefficient on temperature profile. It is noted that both Hartmann and Rayleigh number, angle of inclination and absorption coefficient greatly affects the flow pattern. This therefore means that the aforementioned parameters affect the convective flow of the fluid and thereby affecting the movement of the centered conductor.

1. Effect of angle of inclination on horizontal fluid velocity profile

We hold constant the values of $\text{Rar} = 1000$, and solve equation (14) for values of varying values of ω . Table 1 shows horizontal fluid velocity with varying angle of inclination.

Angle	оf	Chamber length, $x(m)$					
inclination							
$\omega = 45^\circ$		0.0712.35	0.0744 864	0.0750.436	0.0742555	0.0829442	
ω = 60 [°]		0.0740769	0.0811685	0.0830 311	0.0820422	0.0907568	
$\omega = 90^\circ$		0.0755 57	0.0863766	0.0893757	0.0887995	0.0992755	

Table 1. Effect of angle of inclination on horizontal fluid velocity profile

Fig. 2. Effect of angle of inclinition on the horizontal velocity

Fig. 2 gives the influence of angle of inclination on the horizontal velocity profiles. It is observed that the velocity is increased steadily by increasing the angle of inclination. As indicated in the Fig. 2, the flow rate is at its maximum at $\omega = 90$ beyond this value, the velocity component of the flow drops exponentially to zero. Since the angle of inclination is a component of the force of buoyancy, the natural convective flow is high at $\infty = 90$. The fluid velocity is higher at the vertical surface than at the inclined surface since the buoyancy force acts normally on a body.

2. Effect of Rayleigh number on horizontal fluid velocity profile

We hold constant the values of $\omega = 45^0$ and solve equation (14) for values of varying values of Ra_T = 1000, 2000 and 3000 in equation (8), we obtain the solutions of Ra_T as presented in the table 2.

Table 2 shows horizontal fluid velocity with varying Rayleigh number.

Rayleigh number	Chamber length, x					
					Δ	
$Ra_r = 1000$	54.969867	64.39719864	66.10490750	65.56742555	73.35829483	
$Ra_r = 2000$	109.9240769	128.786.853	132.200311	131.1230422	146.7075683	
$Ra_r = 3000$	164.8767.57	193.1704766	198.293755	196.6797998	220.0527557	

Table 2. Effect of Rayleigh number on horizontal fluid velocity profile

The results in Table 2 are represented graphically as shown in Fig. 3.

Fig. 3. Effects of Rayleigh number on horizontal velocity

The effect of Rayleigh number on horizontal fluid velocity can be observed from Fig. 3. An increase in Rayleigh number leads to an increases in the horizontal fluid velocity. This is because the Rayleigh number is a product of force of buoyancy and thereby affecting the free convective part of this occurrence. The result also shows a conducting dominating regime is at low Rayleigh number with vertical velocity profiles since at low Rayleigh number below critical value, there is no fluid flow and heat flow is by conduction and a convective dominating regime is at high Rayleigh number with horizontal velocity profiles. At high Rayleigh number range, the fluid experiences turbulent flow thereby denoting an increased velocity profile.

3. Effect of Rayleigh number on vertical fluid velocity profile

We hold constant the values of $\omega = 45^{\circ}$ and solve equation (17) for values of varying values of Ra_T = 1000, 2000 and 3000 in equation (17), we obtain the solutions of Ra_T as presented in the Table 3.

From fig. 4, it can be concluded that the strength of these vertical velocity profiles increases as the Rayleigh number (Ra) increases this is because Rayleigh number is a product of the bouyancy force.In addition, at high Rayleigh number, the fluid experiences turbulance flow which denotes an increased velocity. The result also shows a conducting dominating regime at low Rayleigh number with vertical velocity profiles and convective dominating regime at high Rayleigh number.

The results in Table 3 are represented graphically as shown graphically in Fig. 4.

Fig. 4. Effects of Rayleigh number on vertical velocity

4. Effects of Hartmann number on vertical velocity profile

We hold constant the values of Ra_T = 1000, ω = 45⁰ and solve equation (17) for values of varying values of Ha = 4, 5 and 6 in equation (17)**,** for varying values of Ha, we obtain solutions as presented in the table 4 below

The results in table 4 are represented graphically as in Fig. 5.

Fig. 5. Vertical velocity against chamber length with varying the Hartman number

From the Fig. 5, it can be concluded that the velocity is influenced by Hartmann number which is a product of the induced Lorentz force. This is due to the formation of a narrower boundary zone, which shows a general trend to induce an electromotive force to the free stream flow of MHD, hence the velocity reduces as shown above. The Lorentz force induced as a result of electrically conducting fluid flow acts against the flow for an applied magnetic field acting in the normal direction as in the current problem. The opposition created lowers the velocity of flow and thereby affecting the general convective current.

5. Effect of dimensionless absorption coefficient on temperature distribution

We varying Φ = 10, 15, and 20 in equation (20). Solving equation (20) for varying values of Φ , we obtain solutions for varying Φ as presented in the table 5 below.

Dimensionless	Chamber length, x					
absorption coefficient	$\mathbf 0$				4	
$\Phi = 10$	6.813856	5.872194	5.5395637	5.1702643	4.0835628	
$\Phi = 15$	6.941472	6.021216	5.6722278	5.3011632	4.172579	
$\Phi = 20$	7.069552	6.170012	5.82 3442	5.4426483	4.263325	

Table 5. F**luid temperature distribution for varying dimensionless absorption coefficient.**

In the Fig. 6, it can be concluded that for certain values of dimensionless absorption coefficient, the surface heat flow tends to decrease by increasing in Φ . This in turn affects the density variation between colder and hotter parts of the fluid. At higher values of Φ, the surface heat transfers or the temperature difference (thermodynamic driving force) tends to decrease thereby lowering the velocity of the flow.

Fig. 6. Temperature against chamber length with varying dimensionless absorption coefficient

The above parameters discussed, strongly affect the fluid flow components which is in agreement with study's objective.

6 Conclusion

A numerical study performed to analyze the influence of the effects; Rayleigh number, Hartmann number, angle of inclination, and absorption coefficient on fluid velocity profiles and temperature distribution. The following outcomes can be deduced from the study:

- An increase in Rayleigh number increases the buoyancy force thereby raising the fluid velocity rate.
- An increase in absorption coefficient lowers the surface heat flow (density variation due to temperature change). Thereby lowering the fluid flow rate.
- The angle of inclination of a conductor directly affects the buoyancy force component, thereby affecting the rate of fluid flow. The buoyancy force increases with an increase in angle of inclination. This factor has an impact on flow rate within a given range values discussed above.
- An increase in Hartmann number lowers the flow rate of fluid. This is due an increase in Lorentz force formed which causes an opposite force to the flow.
- The said findings can be applied in the field of engineering to improve the flow rate of MHD fluids and their extensive application.

Competing Interests

Authors have declared that no competing interests exist.

References

- [1] Nasrin R. Influence of a centered conducting obstacle on MHD Mixed convection in a wavy chamber. The Journal of Naval and Marine Engineering. 2011;8(2).
- [2] Karimipour A, Rozaini R, Abu Bakar N. Magnetic field influenced on combined convection heat flow in a lid – driven rectangular enclosure. Journal of Akademia Baru. 2020; 12:13 – 21.
- [3] Smith TF, House J, Beckermann C. Effects of a centered conducting body on natural convection heat transfer in an enclosure. Numerical heat transfer. Part A. 1990; 18:21 -25.
- [4] Singh AK. Numerical solution of hydro magnetic non-steady natural convection flow past an infinite permeable plate. Indian journal of Pure and Applied Physics. 2002;41(3):167 – 170.
- [5] Sigey JK, Okelo JA, Ngesa J, Gatheri K. Magneto hydrodynamic free convective flow past an infinite vertical porous plate with joule heating. Applied mathematics. 2013;4.
- [6] Sarris IE, Kakarantzas SC, Grecos AP, Vlachos NS. MHD natural convection in a sideways and volumetrically heated square cavity. International Journal of Heat and Mass Transfer. 2005; 48:3443 – 3453.
- [7] Sagheer M, Mehmood K, Hussain S. MHD combined convection and entropy generation of water alumina nano fluid flow in a double lid driven enclosure with discrete heating. Journal of Magnetism and Magnetic Materials. 2010; 419:140 – 155.
- [8] Roy S, Basak T. Finite Element Analysis of free convection flow in a square enclosure with differently heated walls. International journal of Engineering Science. 2005;668 -680.
- [9] Mahdy A., Ahmed S.E., Mansour,M.A. MHD combined convection in a tilted lid driven enclosure with opposing thermal buoyancy force: Influence of non – uniform heating on both side walls. Nuclear Engineering and Design. 2013; 265:931 – 949.
- [10] Oztop H, and Fatih S. Mixed convection of nano fluid filled cavity with oscillating lid under the influence of an inclined magnetic field. Journal of the Taiwan Institute of chemical Engineers. 2016; 63: 200 -225.
- [11] Moreau R, T. Alboussiere and J.P Garandet. Natural convection in a rectangular cavity with a horizontal magnetic field. International Journal of heat mass transfer. 1992; 35:740 – 747.
- [12] Patankar SV. Numerical heat transfers and fluid flow. Hemisphere publishing corporation USA; 2004.
- [13] Sharqawy MH, Zubair SM. Thermophysical properties of sea water; 2010.

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