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# New Equations for Energy Dissipation down a Stepped Spillway

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### Authors' contributions

This work was carried out in collaboration between both authors. Author OO designed the study, performed the statistical analysis, wrote the protocol and wrote the first draft of the manuscript. Author JCA managed the literature searches. Both authors read and approved the final manuscript.

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Original Research Article

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## ABSTRACT

Stepped spillways use their stepping nature to substantially dissipate energy in floodwater. Many researchers investigated the hydraulic and geometric relationships of the stepped spillway with a dam slope above 26.6° degrees that resulted in energy dissipation. But few studied stepped spillways with a dam slope below 26.6° degrees that also resulted in energy dissipation with even fewer proposing models that estimated its energy losses. This resulted in limited information and guidelines for designers of stepped spillways involved with slopes below 26.6° degrees. The authors reviewed researchers' publications on horizontal stepped spillways with dam slopes between  $3.4^\circ \le \theta \le 26.6^\circ$  conducted in transition and skimming flows in large-size facilities with phase-detection intrusive probes. They obtained data sets from them, which they reanalyzed to develop 2 new energy dissipation models that govern skimming flows over a wide range of operating conditions. The data from the new models compared well with the measured data in terms of energy dissipation with high coefficients of correlation between 0.95 and 0.99. All data were in good agreement independent of channel slopes, stepped configuration, and sensor size. The models are simple, easy to use, and render more accurate results than the existing model.

Keywords: Aerated flow; energy dissipation; chute slope; dam height; stepped spillway; skimming flow.

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### ABBREVIATIONS

- *d<sub>c</sub>* : Critical water depth (m)
- Fr : Froude number =  $F_r = \frac{q_w}{\sqrt{gd^3}}$
- H<sub>1</sub> : Residual head at the bottom of the spillway (m)
- $\Delta H$  : Difference between the maximum head and the residual head (m)
- H : Total head (m)
- H<sub>max</sub> : Maximum head available (m)
- $H_{max}$  :  $H_{dam} + 3/2 * d_c$
- Q : Discharge ( $m^2$  s<sup>-1</sup>)
- $q_w$ : Discharge per unit width (m s<sup>-1</sup>) Reynolds number defined as: Re =  $\rho_w * U_w * D_{H'} \mu_w$
- $U_w$  : Flow velocity (m/s):  $U_w = q_w/d$
- W : Channel width (m)

# SUBSCRIPTS

c – Conditions at Critical Height N– Number of Step

### **1. INTRODUCTION**

Major damage may occur if the energy of floodwater, especially its kinetic energy, is not dissipated safely. One type of flood release facility is the stepped spillway. Their steps offer significant resistance to flow that result in energy dissipation. This loss in energy leads to the design of smaller and more economical dissipation structures downstream of the chute. As the discharge down the chute is increased, the critical discharge would be reached, beyond which air would be entrained in the flow. This phenomenon is known as a two-phase flow or Air-Water flow.

Researchers like [1-7] in the last decades, experimentally investigated air-water flows on stepped spillways with a dam slope above 26.6O degrees. They provided vast information and guidelines for its design.

But few studied stepped spillways with a dam slope below 26.60 degrees, which resulted in energy dissipation with fewer proposing models that estimate its energy losses. This resulted in limited information and guidelines for designers of stepped spillways with slopes below 26.60 degrees. There is also a dearth of design rules and publications for stepped spillways; hence, the need for additional study on stepped spillways. Thus, the authors conducted a study that resulted in better equations and provided design engineers with the knowledge of the impact of a stepped spillway on energy dissipation performance.

Essery ITS [8] identified three kinds of flows that occur over a stepped spillway. Such flows include:

a) nappe flow regime, b) transition flow regime, and c) skimming flow regime.

In the nappe flow regime, a sequence of water flows down from one step to the next lower step with the formation of a hydraulic jump at each step. This type of flow can be likened to a sequence of separate drop structures linked together [9,10].

Nappe flow with an established hydraulic jump (Fig. 1) usually occurs from small discharges with shallow flow depths. It flows from one step to the next step below it with the formation of supercritical at the edges of the steps and returns to subcritical flow downstream of the jump at each fall. A hydraulic jump is formed at each drop; energy losses accompany it [3,11]. The losses occur due to

a) The disintegration of the spout in the air [8,12], b) The blending of flow on the steps, with or without the development of hydraulic jump on the step [11].

Energy losses could be computed using equations [1.1] or [1.2].

$$\frac{\Delta H}{H_o} = 1 - \frac{\frac{d_1}{d_c} + \frac{1}{2} \left(\frac{d_c}{d_1}\right)^2}{\frac{3}{2} + \frac{H_{dam}}{d_c}}$$
(1.1)

Where  $d_1$  is the water depth at impact,  $d_c$  is the critical water depth, and  $H_{dam}$  is the dam height,  $\Delta H$  is the energy loss,  $H_o$  is the maximum available energy, h is the height of the spillway step [3] later expressed this equation in terms of the spillway step height, the critical flow depth, and the dam height as:

 $\frac{\Delta H}{H_o} = 1 - \left[ \frac{0.54 \left(\frac{d_c}{h}\right)^{0.275} + \frac{3.43}{2} \left(\frac{d_c}{h}\right)^{-0.55}}{\frac{3}{2} + \frac{H_{dam}}{d_c}} \right]$ (1.2)

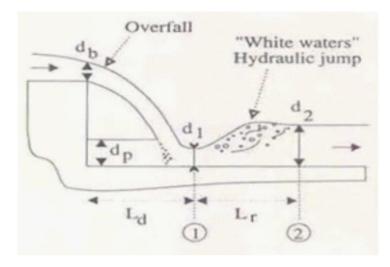


Fig. 1. Nappe flow regime (Flow at a drop structure)

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Several researchers like [13] examined the flow regime change from nappe to skimming in a spillway and linked the parameters to flow critical depth, dc, and the spillway shape, which are the non-dimensional ratios dc /h and h/ l.

Rajaratnam N, [11] took into consideration these non-dimensional parameters and proposed that values of dc/h > 0.8 in the range of 0.42< h/l <0.842 will yield skimming flow, exiting the nappe flow regime when flow rate becomes dc/h < 0.8 whatsoever the geometric specifications of the structure might be.

Studies have, however, shown that the majority of the changes in flow regime occur for the flow rate,  $d_c/h$ , less than this proposed 0.8.

The skimming flow regime occurs with the submergence of the steps with the development of a fully aerated uniform flow downstream of a long chute. Along the upstream steps, a non-aerated flow region exists in which a turbulent boundary layer develops. Air entrainment in the flow begins where the boundary layer intersects the free surface, referred to as the point of inception. Downstream of the point of inception, the flow continues to aerate and varies gradually in depth (Fig. 2). The flow eventually becomes a fully aerated uniform flow in which the water depth, velocity, and air concentration become constant [14,15] (Fig. 3).

Energy is dissipated to keep stable depression vortices. If uniform flow conditions are reached downstream of the spillway, the energy loss could be calculated as follows [15] (Fig. 4):

$$\frac{\Delta H}{H_{max}} = 1 - \frac{\left(\frac{d_w}{d_c}\right)\cos\theta + \frac{1}{2}\left(\frac{d_c}{d_w}\right)^2}{\frac{H_{dam}}{d_c} + \frac{3}{2}}$$
(1.3)

Where  $d_w$  is the clear water depth,  $U_{avg}$  is the average velocity, the total head loss may be rewritten in terms of the friction factor, f, the spillway slope,  $\theta$ , in degree, the critical depth,  $d_c$ , and the dam height,  $H_{dam}$ :

$$\frac{\Delta H}{H_{max}} = 1 - \frac{\left(\frac{f}{8sin\theta}\right)^{1/3}cos\theta + \frac{E}{2}\left(\frac{f}{8sin\theta}\right)^{-2/3}}{\frac{H_{dam}}{d_c} + \frac{3}{2}}$$
(1.4)

Eq [1.4] was computed for spillway slope with  $\theta$  = 52 (degrees) and friction factor, f = 0.3 and f = 1.30, that represent average flow resistance on smooth spillways and stepped spillways, respectively. where E is the kinetic energy correction coefficient,  $\theta$  is the dam slope in degrees.

[5,4,16], Felder S and [17], and [18] have published works on the impact, of scale effects in modeling stepped spillways.

The scale effect is defined as slight misrepresentations, which occur when secondary forces like viscous forces and surface tension forces in turbulent flow are ignored. They are usually overlooked in many open-channel flows. However, if they are ignored in highly air-entrained flows in stepped spillways, where they play significant roles, they could lead to scale effects and wrong interpretations of results [19-22].

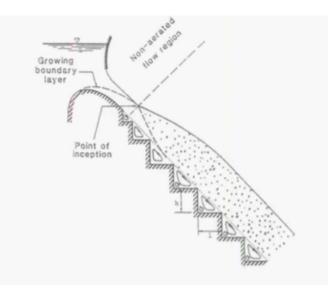


Fig. 2. Skimming flow regime - Sorensen (1985)

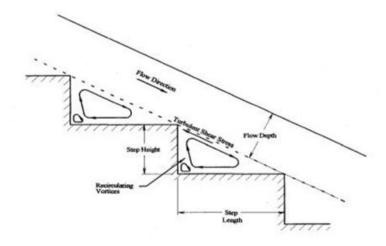


Fig. 3. Skimming flow regime with uniform flow conditions

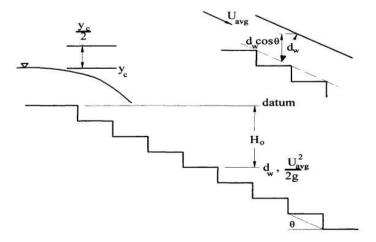


Fig. 4. Arrangement of the spillway with the definition of the variables

Scale effects in stepped spillway models are likely to occur with scales lower than 10:1, Reynolds number smaller than 1 x  $10^5$ , Weber number smaller than 100, and step heights lesser than 3 cm.

### 2. MATERIALS AND METHODS

The authors carefully selected from the literature 11 No publications (listed in Table 1) on horizontal stepped spillways with minimum step heights of 3 cm, undistorted Froude values, and large dimensionless discharges corresponding to Reynolds numbers between  $1 \times 105$  and  $1 \times 10^6$ .

The researchers used experimental facilities on large scale to minimize scale effects that affect the air-water flow processes in high-velocity freesurface flows [17]. They measured air-water flow properties at all step edges downstream of the inception point of air-entrainment with conductivity phase-detection intrusive probes and optical fiber probes.

Use of a Dall Tube flow meter, or V-notch for flow rates, Prandtl-Pitot for flow velocities, or Point gauge for clear water flow depth to obtain airwater flows properties is not practicable as large quantities of air are entrained at the air-water interface [23,24].

The principle of the conductivity probe is based on the difference between the resistivity of air and water, which provides an instantaneous voltage signal [25,26]. The threshold technique analyzes signals - from a single sensor - used to calculate a) the time-averaged local air concentration or void fraction C, b) the number of air-to-water (or water-to-air) voltage changes expressed as bubble count rate F, and c) the air bubble and water droplet chord sizes. For a double-tip conductivity probe with longitudinal separation between the two probe sensors, the cross-correlation analysis of the signals leads to the local time-averaged interfacial velocity V [15].

Details about signal processing techniques can be found in [10] and [27].

The double-tip conductivity probes used had sensor sizes of  $\emptyset$  = 0.13 mm and 0.25 mm and

were sampled for a period of 45 s with a frequency of 20 kHz per sensor.

The discharges comprised transition and skimming flow rates  $0.035 \le q_w \le 0.234$  m2/s for the spillways with  $\theta = 8.9^{\circ}$  and  $0.02 \le q_w \le 0.249$  m2/s for  $\theta = 26.6^{\circ}$  comprising Reynolds numbers of  $1.4 \times 10^5 \le \text{Re} \le 9.3 \times 10^5$  and  $8.1 \times 10^4 \le \text{Re} \le 9.9 \times 10^5$  (Table 1).

Table 1 lists the selected publications, the channel slope, the step height h, the channel width W, the flow rate per unit width  $q_w$ , the flow rate  $d^c/h$  with dc the critical flow depth.

### 2.1 Formulation of the Models

The authors obtained more than 700 data sets from the 11 No researchers (Table 1). They reanalyzed about 500 with complete data to formulate energy dissipation models that govern transition and skimming flow over a wide range of operating conditions.

In modeling, it is necessary to determine the values of the parameters that can fit the model of the system it shall describe [28]. By the least square method, the best fit curve for this study was as:

$$\frac{\Delta H}{H_{max}} = \left[\alpha_o \frac{Nh}{y_c}\right]^{\alpha_1} N^{\alpha_2} h^{\alpha_2} \theta^{\alpha_3}$$
(2.1)

Where

 $\frac{\Delta H}{H_{max}}$  is the energy loss ratio, H<sub>max</sub> is the maximum available height, N is the number of spillway steps, h is the height of the spillway steps,  $\theta$  is the spillway channel slope.

They used a portion of the measured data sets and multiple regression analysis to solve Equation [2.1] which yielded the values of the constant  $\alpha_o$  along with the coefficients  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_3$ , and  $\alpha_4$ , which are then substituted in Equation [2.1] to give the developed models in 3.1.

They used the remaining portion to evaluate the model's performance.

References	Slope ( $\theta$ )deg	Step geometry and Flow conditions	Instrumentation	N (No of Step)
[29]	21.8	h (cm) = 10	Double-tip	10
		dc/h = 1.0 −1.57	(Ø=0.25mm)	
		qw (m²/s)= 0.095-0.18	20kHz/45s	
		$Re = 3.8x10^5 - 7.2x10^5$		
[30]	21.8	h (cm) = 5	Double-tip	20
		dc/h = 1.17 - 3.16	(Ø=0.25mm)	
		qw (m²/s)= 0.059 - 0.10	20kHz/45s	
		$Re = 2.4x10^5 - 4.0x10^5$		
[31]	26.6	h (cm) = 10	Double-tip	10
		dc/h = 0.5 - 1.7	(Ø=0.025mm)	
		qw (m²/s)= 0.03 - 0.217	20kHz/45s	
		$Re = 1.2x10^5 - 8.7x10^5$		
[32]	3.4	h (cm) = 14.3	N/A	10
		dc/h = 0.61 - 0.92		
		qw (m²/s) = 0.08 - 0.15		
		$Re = 3.2x10^5 - 6.0x10^5$		
[33]	18.4 &	h (cm) = 3 & 6	N/A	2.4 m
	26.6	dc/h = 2.65 - 3.58		H <sub>dam</sub>
		qw (m²/s)= 0.07 - 0.11		
		$Re = 2.8x10^5 - 4.4x10^5$		
[34]	3.4	h (cm) = 7.15 & 11.3	Single-tip	10
		dc/h = 0.61 - 1.85	(Ø=0.35mm)	&
		qw (m²/s) = 0.08 - 0.15	5kHz/60s & 180s	18
		$Re = 3.2x10^5 - 6.0x10^5$		
[35]	5.7	h (cm) = 0.63 & 5.0	Single-tip	
	&	dc/h = 1.25 - 14.3	(Ø=0.1mm)	
	11.3	qw (m²/s)= 0.02 - 0.08	2kHz/60s	
		$Re = 0.8x10^5 - 3.2x10^5$		
[36]	14.6	h (cm) = 5 & 10	Double-tip	26
		dc/h =1.27 - 3.55	(Ø=0.13mm)	
		qw (m²/s)= 0.05 - 0.234	30kHz/40s ′	
		$Re = 2.0x10^5 - 9.4x10^5$		

# Table 1. Summary of the 11 No Publications for the flat stepped spillway with chute angle of $3.4^{\circ} \le \theta \le 26.6^{\circ}$

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References	Slope ( $\theta$ )deg	Step geometry and Flow conditions	Instrumentation	N (No of Step)
[34]	15.9	h (cm) = 10	Double-tip	9
	&	dc/h = 0.78 - 1.53	(Ø=0.025mm)	
	21.8	qw (m²/s)=0.069 – 0.188	20kHz/20s	
		$Re = 2.8x10^5 - 7.5x10^5$		
[37]	15.9	h (cm) = 5 & 10	Double-tip	9
		dc/h = 0.6 - 3.2	(Ø=0.025mm)	&
		qw (m <sup>2</sup> /s)= 0.021 - 0.22	20kHz/20s	18
		$Re = 5.0x10^5 - 8.8x10^5$		
[38]	18.4	h (cm) = 3 & 6	Double-tip	2.4 m
	&	dc/h = 2.65 – 3.58	(Ø=0.13mm)	H <sub>dam</sub>
	26.6	qw (m²/s)= 0.07 - 0.11	25kHz/25s	
		$Re = 2.8x10^5 - 4.4x10^5$		
[37]	21.8	h (cm) = 10	Double-tip	10
		dc/h = 1.1 - 1.7	(Ø=0.025mm)	
		qw (m²/s)= 0.114 - 0.22	20kHz/20s	
		$Re = 4.6x10^5 - 8.8x10^5$		
[18]	8.9	h (cm) = 5	Double-tip	21
		dc/h = 1.0 - 3.55	(Ø=0.13mm)	
		qw (m²/s)=0.035 – 0.234	20kHz/45s	
		$Re = 1.4x10^5 - 9.4x10^5$		
[18]	26.6	h (cm) = 5 & 10	Double-tip	10
		dc/h = 0.69 - 3.30	(Ø=0.25mm)	&
		qw (m <sup>2</sup> /s)= 0.02 – 0.227	20kHz/45s	20
		$Re = 0.8x10^5 - 9.1x10^5$		
[18]	26.6	h (cm) = 10	Double-tip	20
		dc/h = 0.82 – 1.85	(Ø=0.25mm)	
		$qw(m^2/s) = 0.073 - 0.249$	20kHz/45s	
		$Re = 2.9 \times 10^5 - 1.0 \times 10^6$		

### 3. RESULTS AND DISCUSSION

### 3.1 Developed Models for Skimming Flow Regimes

**3.1.1** Eq [3.1] is valid for use when h (cm) is not more than 20, N is not more 20,  $\theta$  (degrees) is between 26.6° and 21.8°, and d<sub>o</sub>/h is between 1.0 and 3.7.

$$\frac{\Delta H}{H_{max}} = \left[0.049 \frac{Nh}{d_c}\right]^{0.353} N^{0.06} h^{0.124} \theta^{-0.157} \qquad (3.1)$$

**3.1.2** Eq [3.2] is valid for use when h (cm) is not more than 20, N is not more 20,  $\theta$  (degrees) is between 21.8° and 3.4°, and d<sub>c</sub>/h is between 1.0 and 3.6.

$$\frac{\Delta H}{H_{max}} = \left[0.029 \frac{Nh}{d_c}\right]^{0.353} N^{0.06} h^{0.124} \theta^{-0.157} \quad (3.2)$$

#### 3.2 Charts for 3.1.1

Figs. 5 to 8 depicted the energy loss rates as a function of the expression of a dam height divided by the critical depth for the measured data, the developed analytical formulation (Eq. [3.1]), the existing model for the computation of energy dissipation (Eq. [1.4]) with the friction factors of f = 0.30 and 1.30. The figures also show some traditional concave shape distributions for all the plotted four data sets for energy dissipation for all the flow rates. As seen in the charts, energy losses increase with decreasing discharges and increase with increasing spillway height following earlier investigations [6,35,3]. The measured data and the developed model data (Eq. [3.1]) are in close agreement with the coefficients of correlation from 0.96 to 0.99. Again, measured data are in close agreement with the existing model data (Eq. [1.4]) with a friction factor, f = 0.3, yielding the coefficients of correlation between 0.92 and 0.95

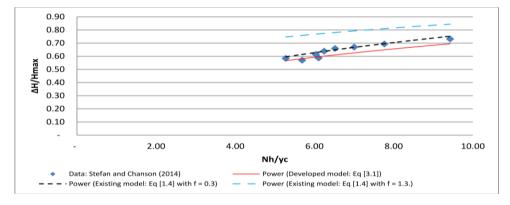


Fig. 5.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 26.6, N = 10, h= 10, q<sub>w</sub> = (0.073 - 0.249) m<sup>2</sup> s<sup>-1</sup> & Re = (2.92 x 10<sup>5</sup> - 9.96 x 10<sup>5</sup>), flow rate d<sub>c</sub>/h of (0.82 - 1.85).

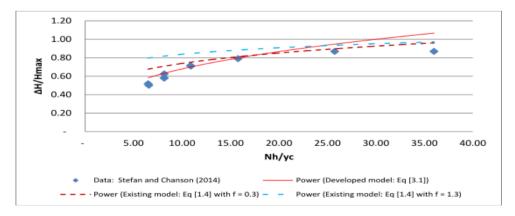


Fig. 6.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 26.6, N = 20, h = 5, q<sub>w</sub> = (0.020 - 0.227) m<sup>2</sup> s<sup>-1</sup> & Re = (8.0 x 10<sup>4</sup> - 9.08 x 10<sup>5</sup>), flow rate d<sub>c</sub>/h, of (0.69 - 3.30).]

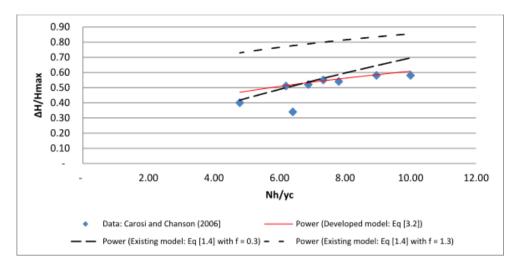


Fig. 7.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 21.8, N = 10, h = 10, q<sub>w</sub> = (0.095 - 0.180) m<sup>2</sup> s<sup>-1</sup>, Re = (3.80 x 10<sup>5</sup> - 7.20 x 10<sup>5</sup>), flow rate, dc/h, of (1.00 - 1.57)

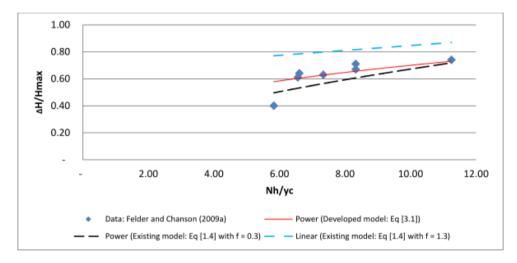


Fig. 8.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 21.8, N = 20, h = 5, q<sub>w</sub> = (0.059 - 0.158) m<sup>2</sup> s<sup>-1</sup>, Re = (2.36 x 10<sup>5</sup> - 6.32 x 10<sup>5</sup>), flow rate, d<sub>c</sub>/h, of (0.80 - 1.85)

### 3.3 Charts for 3.1.2

Figs. 9 to 14 depicted the energy loss rates as a function of the expression of a dam height divided by the critical depth for the measured data, the developed analytical formulation (Eq. [3.2]), the existing model for the computation of energy dissipation (Eq. [1.4]) with f = 0.10, 0.30, and 1.3. They displayed similar traditional concave shape distributions for all plotted four data sets for energy dissipation for all flow rates. As shown in the charts, energy losses increase with decreasing discharges and increase with heights risina dam that follow earlier investigations [6,34,3]. They showed that measured data sets, the developed model data

(Eq. [3.2]), and the existing model data (Eq. [1.4]) with friction factor, f = 0.3, are in close agreement with the coefficients of correlation from 0.95 to 0.99. Fig. 9 showed that the developed model data (Eq [3.2]) was slightly higher than the measured data, increasing with increasing discharges. Fig. 10 indicated that the developed model compared well with the measured data than the existing model with f =0.10. Figs. 11, 12, and 13 showed that the developed model compared well with the measured data sets. Fig. 14 shows that the developed model predicted values slightly lower than the measured data, while the existing model with f = 0.10 produced data sets higher than the measured data sets.

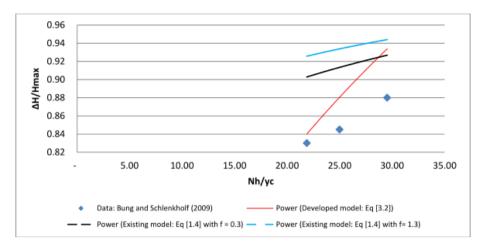


Fig. 9.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 18.4, N=40, h = 6, q<sub>w</sub> = (0.059 - 0.158m) m<sup>2</sup> s<sup>-1</sup>, Re = (2.36 x 10<sup>5</sup> - 6.32 x 10<sup>5</sup>), flow rate, d<sub>c</sub>/h, of (0.80 - 1.85)

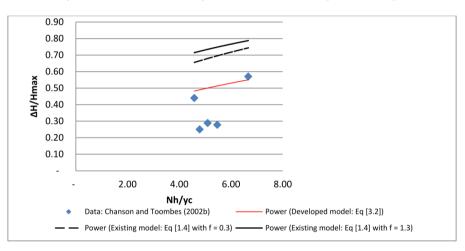


Fig. 10.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  =15.9, N = 9, h = 10, q<sub>w</sub> = (0.069 - 0.188) m<sup>2</sup> s<sup>-1</sup>, Re = (2.76 x 10<sup>5</sup> - 7.52 x 10<sup>5</sup>), flow rate, dc/h, of (0.78 - 1.53)

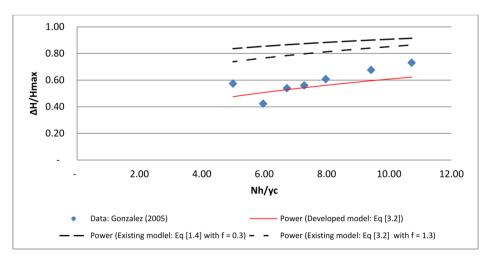


Fig. 11.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 15.9, N = 18, h = 5, q<sub>w</sub> = (0.021 - 0.220) m<sup>2</sup> s<sup>-1</sup>, Re = (8.4 x 10<sup>3</sup> - 8.8 x 10<sup>5</sup>), & flow rate, dc/h of (0.60 - 3.20)

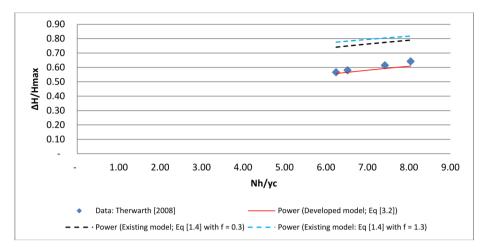


Fig. 12.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 14.6, N = 13, h = 10, q<sub>w</sub> = (0.05 - 0.234) m<sup>2</sup> s<sup>-1</sup>, Re = (2.0 x 10<sup>5</sup> - 9.36 x 10<sup>5</sup>), & flow rate, dc/h, of (1.27 - 3.55)

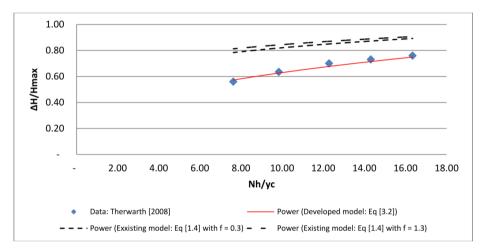


Fig. 13.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 14.6, N = 26, h = 10.0, q<sub>w</sub> = (0.05 - 0.234) m<sup>2</sup> s<sup>-1</sup>, Re = (2.0 x 10<sup>5</sup> - 9.36 x 10<sup>5</sup>), & flow rate, d<sub>c</sub>/h, of (1.27 - 3.55)

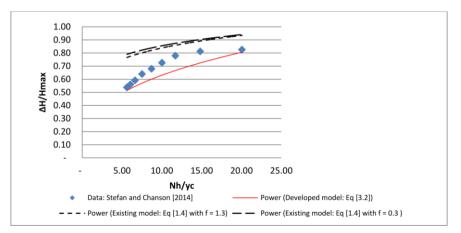


Fig. 14.  $\Delta$ H/H<sub>max</sub> as a function of Nh/d<sub>c</sub> for  $\theta$  = 8.9, N = 21, h = 3, q<sub>w</sub> = (0.035 - 0.234) m<sup>2</sup> s<sup>-1</sup>, Re = (1.40 x 10<sup>5</sup> - 9.36 x 10<sup>5</sup>), & flow rate, dc/h, of (1.0 - 3.55)

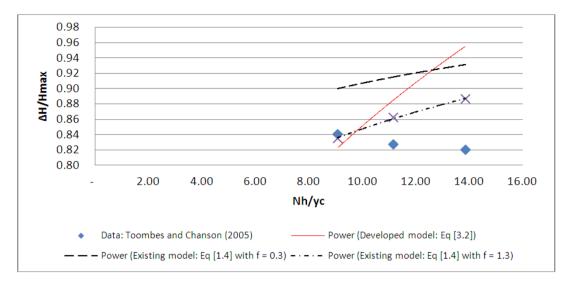


Fig. 15.  $\Delta$ H/H<sub>max</sub> as a function of Nh/dc for q<sub>w</sub> = (0.61 - 0.92m<sup>2</sup>/s), Re = (2.44 x 10<sup>6</sup> - 3.68 x 10<sup>6</sup>), & flow rate, dc/h, of 0.82 - 1.85

Fia. 15 showed interestina pattern: an Rates of energy losses with a stepped spillway slope of 3.4° degrees reduced along the spillwav with decreasing discharges and decreased with increasing stepped spillway height.

So, there is a need to investigate further why this incidence occurred in future.

## 4. CONCLUSION

Two new models for rates of energy losses in horizontal stepped spillways with slopes below 26.60 degrees, with data based on detailed phase-detection probe measurements were developed. Their generated data compared well with the measured data sets. The new models also produced data sets that were in close agreement with the existing equation for rates of energy losses with friction factor, f = 0.10. Rates of energy losses increased along the stepped with decreasing discharges and spillway increased with increasing stepped spillway heights. However, rates of energy losses with a stepped spillway slope of 3.40 degrees decreased along the spillway with decreasing discharges and decreased with increasing stepped spillway height.

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### **COMPETING INTERESTS**

Authors have declared that no competing interests exist.

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